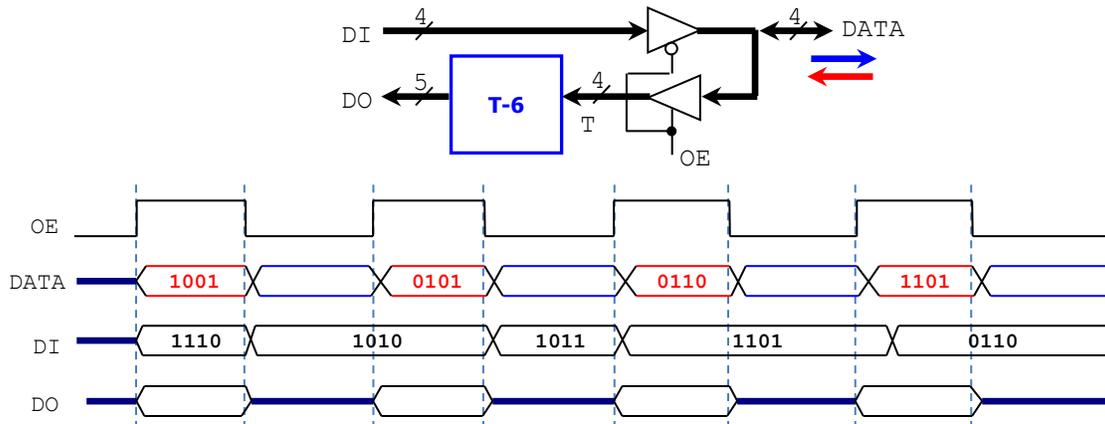


PROBLEM 3 (12 PTS)

- Complete the timing diagram (signals *DO* and *DATA*) of the following circuit. The circuit in the blue box computes the signed (2C) operation T-6, with the result having 5 bits. T is a 4-bit signed (2C) number.
For example: if $T=1010 \rightarrow DO = 1010 - 0110 = 11010 + 11010 = 10100$.



PROBLEM 4 (37 PTS)

- a) Perform the following additions and subtractions of the following unsigned integers. Use the fewest number of bits n to represent both operators. Indicate every carry (or borrow) from c_0 to c_n (or b_0 to b_n). For the addition, determine whether there is an overflow. For the subtraction, determine whether we need to keep borrowing from a higher bit. (8 pts)

Example ($n=8$):

✓ $210 + 54$

$$\begin{array}{r}
 \begin{array}{cccccccc}
 c_8 & c_7 & c_6 & c_5 & c_4 & c_3 & c_2 & c_1 & c_0 \\
 & & & & & & & & \\
 54 = 0 \times 36 = & 0 & 0 & 1 & 1 & 0 & 1 & 1 & 0 & + \\
 210 = 0 \times D2 = & 1 & 1 & 0 & 1 & 0 & 0 & 1 & 0 & \\
 \hline
 \text{Overflow!} \rightarrow & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0
 \end{array}
 \end{array}$$

✓ $77 - 194$

$$\begin{array}{r}
 \text{Borrow out!} \rightarrow \begin{array}{cccccccc}
 b_8 & b_7 & b_6 & b_5 & b_4 & b_3 & b_2 & b_1 & b_0 \\
 & & & & & & & & \\
 77 = 0 \times 4D = & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 1 & - \\
 194 = 0 \times C2 = & 1 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & \\
 \hline
 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 1 &
 \end{array}
 \end{array}$$

- ✓ $165 + 89$
- ✓ $109 + 53$

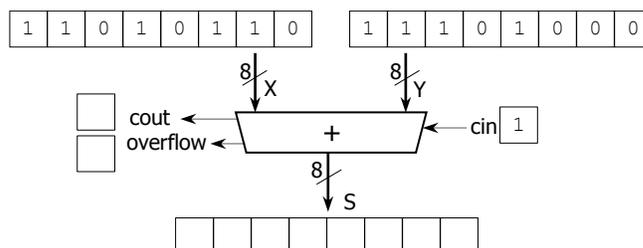
- ✓ $194 - 125$
- ✓ $93 - 129$

- b) We need to perform the following operations, where numbers are represented in 2's complement (2C): (20 pts)

- ✓ $358 + 157$
- ✓ $109 - 146$
- ✓ $-91 + 125$
- ✓ $-66 - 127$
- ✓ $87 - 46$

- For each case:
 - ✓ Determine the minimum number of bits n required to represent both summands. You might need to sign-extend one of the summands, since for proper summation, both summands (and the result) must have the same number of bits.
 - ✓ Perform the signed (2C) binary addition, i.e., complete all the carries (c_0 to c_n) and the summation bits (s_0 to s_{n-1}).
 - ✓ Determine whether there is overflow by:
 - Using c_n, c_{n-1} (carries).
 - Performing the operation in the decimal system and checking whether the result is within the allowed range for n bits, where n is the minimum number of bits for the summands.
 - ✓ If we want to avoid overflow, what is the minimum number of bits required to represent both the summands and the result?

- c) For the following 8-bit 2's complement adder, complete all the outputs (S, cout, overflow) given the input values. (3 pts)



- d) Get the multiplication results of the following numbers that are represented in 2's complement arithmetic with 4 bits. (6 pts)
- ✓ 0101×0101 , 1011×0111 , 1010×1110 .